# Cavanaugh Macdonald 

CONSULTING, LLC

The experience and dedication you deserve


EMPLOYEES'
RETIREMENT SYSTEM
OF GEORGIA

GEORGIA PUBLIC SCHOOL EMPLOYEES' RETIREMENT SYSTEM

EXPERIENCE INVESTIGATION FOR THE FIVE-YEAR PERIOD ENDING JUNE 30, 2014


# Cavanaugh Macdonald <br> C O N SULTIN G, LLC <br> The experience and dedication you deserve 

December 17, 2015
Board of Trustees
Georgia Public School Employees’ Retirement System
Two Northside 75, Suite 300
Atlanta, GA 30318
Members of the Board:

We are pleased to submit the results of an investigation of the economic and demographic experience for the Georgia Public School Employees' Retirement System. The purpose of the investigation was to assess the reasonability of the actuarial assumptions currently used by the Retirement System. This investigation covers the five-year period from July 1, 2009 to June 30, 2014. As a result of the investigation, it is recommended that revised economic and demographic tables be adopted by the Board for future use.

The investigation of the demographic experience of members of the System includes all active and retired members as well as beneficiaries of deceased members. The experience was investigated separately for males and females since different tables are used for each of these groups.

The number of members expected to separate from active service and the expected number of postretirement deaths was obtained by use of the rates determined in the last experience investigation and adopted by the Board of Trustees. The results of the investigation indicate that the assumed rates of separation from active service due to withdrawal, death and retirement, and the rates of post-retirement mortality do not accurately reflect the actual and anticipated experience of the Retirement System. As a result of the investigation, new withdrawal, retirement and mortality tables have been developed which reflect more closely the actual experience of the membership.

This report shows a comparison of the actual and expected cases of separation from active service and actual and expected number of deaths. A comparison between the rates of separation and mortality presently in use and the recommended revised rates are also shown in this report.

All new assumptions are shown in the attached tables in Appendix C of this report. In the actuary's judgment, the recommended assumptions are suitable for use until further experience indicates that modifications are desirable.

The experience investigation was performed by, and under the supervision of, independent actuaries who are members of the American Academy of Actuaries with experience in performing valuations for public retirement systems. The undersigned meet the Qualification Standards of the American Academy of Actuaries to render the actuarial opinion contained herein.

Respectfully submitted,


Edward A. Macdonald, ASA, FCA, MAAA President


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Principal and Managing Director

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Principal and Consulting Actuary

## TABLE OF CONTENTS

Section Page
I Executive Summary ..... 1
II Financial Impact ..... 3
III Economic Assumptions ..... 4
IV Demographic Assumptions ..... 11
Rates of Withdrawal ..... 12
Rates of Disability Retirement ..... 18
Rates of Retirement ..... 19
Rates of Pre-Retirement Mortality ..... 23
Rates of Post-Retirement Mortality ..... 26
V Other Assumptions and Methods ..... 32
Appendix
A Historical June CPI (U) Index ..... 33
B Capital Market Assumptions and Asset Allocation ..... 34
C Recommended Rates ..... 35

## Section I Executive Summary

The following table summarizes the findings and recommendations with regard to the assumptions utilized for the Georgia Public School Employees' Retirement System. Detailed explanations for the recommendations are found in the sections that follow.

## Recommended Economic Assumption Changes

The table below lists the two economic assumptions used in the actuarial valuations and the current and proposed rates.

| Item | Current | Proposed |
| :--- | :---: | :---: |
| Price Inflation | $3.00 \%$ | $2.75 \%$ |
| Investment Return* | $7.50 \%$ | $7.50 \%$ |

* net of investment expenses.


## Recommended Demographic Assumption Changes

The table below lists the demographic assumptions we recommend be changed based on the experience of the last five years.

## Assumption Changes

Withdrawal, Pre-Retirement Mortality, Service Retirement and Post-Retirement Mortality

## Recommended Other Assumption Changes

The table below lists the other assumptions that are considered in our valuations that should be reviewed during the experience study.

| Assumption | Assumption Changes |
| :--- | :---: |
| Administrative Expenses | No Change to current method of determining rate |
| Amortization Method | No change to current method of level dollar <br> amortization |
| Asset Smoothing | No change to current method of smoothing market <br> gains and losses over 5 year period |
| No change to current assumption of 1.5\% semi-annually |  |
| Option Factors Living | Recommend change in current option factors to reflect <br> change in mortality rate |
| Termination Benefits change in assumption for active vested |  |
| Valuation Cost Method | No change in Entry Age Normal Cost Method |

## Section II <br> Financial Impact

The following table highlights the impact of the recommended changes on the principal valuation results.

## Impact on Principal Valuation Results

| Valuation Results | Recommended |
| :---: | :---: |
| 2014 | Assumptions |

Unfunded Accrued
Liability \$158,915,410 \$189,416,143

| Funding Ratio | $82.8 \%$ | $80.2 \%$ |
| :--- | :---: | :---: |
|  |  |  |
| Actuarially Determined <br> Employer Contribution |  |  |
| $\quad$ Normal Cost* | $\$ 11,779,000$ | $\$ 13,063,000$ |
| Accrued Liability <br> Total | $\underline{\$ 14,498,000}$ | $\$ 17,234,000$ |
|  | $\$ 26,277,000$ | $\$ 30,297,000$ |

Amortization Period

| (in years) | 23.9 | 24.0 |
| :--- | :--- | :--- |

*Normal Cost includes estimated administrative expenses

## Section III Economic Assumptions

There are two economic assumptions used in the actuarial valuations performed for the System. They are:

- Price Inflation
- Investment Return

Actuarial Standard of Practice (ASOP) No. 27, "Selection of Economic Assumptions for Measuring Pension Obligations" provides guidance to actuaries in selecting economic assumptions for measuring obligations under defined benefit plans. ASOP No. 27 was revised in September, 2013 and no longer includes the concept of a "best estimate range". Instead, the revised standard now requires that each economic assumption selected by the actuary should be reasonable which means it has the following characteristics:

- It is appropriate for the purpose of the measurement;
- It reflects the actuary's professional judgment;
- It takes into account historical and current economic data that is relevant as of the measurement date;
- It reflects the actuary's estimate of future experience, the actuary's observation of the estimates inherent in market data, or a combination thereof; and
- It has no significant bias (i.e., it is not significantly optimistic or pessimistic), except when provisions for adverse deviation or plan provisions that are difficult to measure are included and disclosed, or when alternative assumptions are used for the assessment of risk.

Each economic assumption should individually satisfy this standard. Furthermore, with respect to any particular valuation, each economic assumption should be consistent with every other economic assumption over the measurement period.

In our opinion, the economic assumptions recommended in this report have been developed in accordance with ASOP No. 27. The following table shows our recommendations followed by detailed discussions of each assumption.

| Item | Current | Proposed |
| :--- | :--- | :--- |
| Price Inflation | $3.00 \%$ | $2.75 \%$ |
| Real Rate of Return* | $\underline{4.50}$ | $\underline{4.75}$ |
| Investment Return | $7.50 \%$ | $7.50 \%$ |

[^0]
## Price Inflation

Background: As can be seen from the table on the previous page, assumed price inflation is used as the basis for the investment return assumption. This latter assumption will be discussed in detail in the following section.

It is important that the price inflation assumption be consistently applied throughout the economic assumptions utilized in an actuarial valuation. This is called for in ASOP No. 27 and is also required to meet the parameters for determining pension liabilities and expense under Governmental Accounting Standards Board (GASB) Statements No. 67 and 68.

The current price inflation assumption is $3.00 \%$ per year.

Past Experience: The Consumer Price Index, US City Average, All Urban Consumers, CPI (U), has been used as the basis for reviewing historical levels of price inflation. The level of that index in June of each of the last 50 years is provided in Appendix A.

In analyzing this data, annual rates of inflation have been determined by measuring the compound growth rate of the $\mathrm{CPI}(\mathrm{U})$ over various time periods. The results are as follows:

| Period | Number of <br> Years | Inflation | Annual <br> Standard Deviation |
| :---: | :---: | :---: | :---: |
| $2004-2014$ | 10 | $2.31 \%$ | $1.81 \%$ |
| $1994-2004$ | 10 | 2.51 | 0.83 |
| $1984-1994$ | 10 | 3.62 | 1.06 |
| $1974-1984$ | 10 | 7.78 | 3.39 |
| $1964-1974$ | 10 | 4.68 | 2.63 |
| $1994-2014$ | 20 | $2.41 \%$ | $1.37 \%$ |
| $1984-2014$ | 30 | 2.81 | 1.39 |
| $1974-2014$ | 40 | 4.03 | 2.99 |
| $1964-2014$ | 50 | 4.16 | 2.90 |
| $1926-2014$ | 88 | 2.98 | 4.15 |

The following graph illustrates the historical levels of price inflation measured as of June 30th of each of the last 50 years and compared to the current $3.00 \%$ annual rate currently assumed.

Annual Rate of CPI (U) Increases


Over more recent historical periods, the average annual rate of increase in the CPI-U has been below $3.00 \%$. The period of high inflation from 1973 to 1982 has a significant impact on the averages over periods which include these rates. Further, the average rate of $2.98 \%$ over the entire 88 year period is close to the average rate of $2.81 \%$ for the prior 30 years (1984 to 2014) but the volatility of the annual rates in the more recent years has been markedly lower as indicated by the significantly lower annual standard deviations. Many experts attribute the lower average annual rates and lower volatility to the increased efforts of the Federal Reserve since the early 1980's to stabilize price inflation. The severe recession of 2008-2009 resulted in a short period of deflation followed by low levels of inflation. The Federal Reserve has combated this weak environment with zero interest rates and quantitative easing. Although the quantitative easing program has ended, the Federal Reserve has disclosed an inflation target of at least $2.0 \%$ annually and will keep interest rates very low until they see progress toward the target.

Recommendation: It is difficult to accurately predict inflation. Inflation's short-term volatility is illustrated by comparing its average rate over the last 10,30 and 50 years. Although the 10 -year average of $2.31 \%$ is lower than the System's assumed rate of $3.00 \%$, the longer 30, 40 and 50 -year averages of $2.79 \%, 3.94 \%$ and $4.25 \%$ respectively, are at or slightly higher than the System's rate. The validity of the System's assumption is, therefore, dependent upon the emphasis one assigns to the short and long-terms.

Current economic forecasts suggest lower inflation but are generally looking at a shorter time period than appropriate for our purposes. In the 2014 OASDI Trustees Report, the Chief Actuary for Social Security bases the 75 year cost projections on an intermediate inflation assumption of $2.7 \%$ with a range of $1.7 \%$ to $3.7 \%$. We consider that range reasonable, and recommend that PSERS lower the current price inflation assumption from 3.00 to $2.75 \%$ per year.

## Price Inflation Assumption

Current 3.00\%

Recommended
$2.75 \%$

## Investment Return

Background: The assumed investment return is one of the most significant assumptions in the annual actuarial valuation process as it is used to discount the expected benefit payments for all active, inactive and retired members of the System. Minor changes in this assumption can have a major impact on valuation results. The investment return assumption should reflect the asset allocation target for the funds set by the Board of Trustees.

The current assumption is $7.50 \%$, consisting of a price inflation assumption of $3.00 \%$ and a real rate of return assumption of $4.50 \%$. The return is net of all investment expenses.

Past Experience: The assets for the System are valued using a widely accepted asset-smoothing methodology (5-year smoothing) that fully recognizes the expected investment income and also recognizes $20 \%$ of each year's investment gain or loss (the difference between actual and expected investment income). The asset smoothing methodology from 2010 through 2012 was based on 7-year smoothing and actuarial value was set equal to market value in 2013. The recent experience over the last five years is shown in the table below.

| Year <br> Ending <br> 6/30 | Actuarial Value | Market Value <br> Rate of Return |
| :---: | :---: | :---: |
| 2010 | $2.17 \%$ | $11.59 \%$ |
| 2011 | 4.14 | 21.65 |
| 2012 | 4.37 | 2.00 |
| 2013 | 6.84 | 13.45 |
| 2014 | 9.47 | 17.37 |
| Average | $5.37 \%$ | $13.02 \%$ |

The impact of the asset smoothing method can be observed in the table. Very poor asset returns during 2008 and 2009 are reflected in the actuarial value returns through 2013. While important to review and analyze, historical returns over such a short time period are not credible for the purpose of setting the long-term assumed future rate of return.

We next include in our analysis information concerning future expectations for the investment return assumption. Because of the significant variability in past year-to-year results and the interplay of inflation on those results in the short term, we prefer to base our investment return assumption on the capital market assumptions utilized by the Board in setting investment policy and the asset allocation established by the Board as a result of that policy. This approach is referred to as the building block method in ASOP No. 27.

Analysis: The current capital market assumptions and asset allocation as provided by the System are shown in Appendix B. We further assumed that investment returns approximately follow a lognormal distribution with no correlation between years. The results below provide an expected range of real rates of return over a 50 year time horizon. Looking at one year results produces an expected real return of $6.38 \%$ but also has a high standard deviation or measurement of volatility. By expanding the time horizon, the average return does not change much but the volatility declines significantly. The following table provides a summary of results. The geometric real rates of return are net of investment expenses.

| Time <br> Span In <br> Years | Mean <br> Real <br> Return | Standard <br> Deviation | $\mathbf{5}^{\text {th }}$ |  |  |  |  |  | Real Returns by Percentile |  |  |  |
| :---: | :---: | ---: | ---: | ---: | ---: | ---: | ---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $6.38 \%$ | $15.36 \%$ | $-16.87 \%$ | $-4.44 \%$ | $5.29 \%$ | $16.00 \%$ | $33.35 \%$ |  |  |  |  |  |
| 5 | $5.51 \%$ | $6.79 \%$ | $-5.27 \%$ | $0.82 \%$ | $5.29 \%$ | $9.95 \%$ | $17.02 \%$ |  |  |  |  |  |
| 10 | $5.40 \%$ | $4.79 \%$ | $-2.29 \%$ | $2.11 \%$ | $5.29 \%$ | $8.56 \%$ | $13.46 \%$ |  |  |  |  |  |
| 20 | $5.34 \%$ | $3.38 \%$ | $-0.13 \%$ | $3.03 \%$ | $5.29 \%$ | $7.59 \%$ | $11.00 \%$ |  |  |  |  |  |
| 30 | $5.32 \%$ | $2.76 \%$ | $0.84 \%$ | $3.44 \%$ | $5.29 \%$ | $7.17 \%$ | $9.93 \%$ |  |  |  |  |  |
| 40 | $5.32 \%$ | $2.39 \%$ | $1.43 \%$ | $3.69 \%$ | $5.29 \%$ | $6.91 \%$ | $9.30 \%$ |  |  |  |  |  |
| 50 | $5.31 \%$ | $2.14 \%$ | $1.93 \%$ | $3.86 \%$ | $5.29 \%$ | $6.74 \%$ | $8.87 \%$ |  |  |  |  |  |

Based on this analysis there is a $50 \%$ likelihood that the average real rate of return over a 50 -year period will be $5.29 \%$. it can also be inferred that for the 10 year time span, $5 \%$ of the resulting real rates of return were below $-2.29 \%$ and $95 \%$ were above that. As the time span increases, the results begin to merge. Over a 50 year time span, the results indicate there is a $25 \%$ chance that real returns will be below $3.86 \%$ and a $25 \%$ chance they will be above $6.74 \%$. In other words there is a $50 \%$ chance the real returns will be between $3.86 \%$ and $6.74 \%$.

Recommendation: Using the building block approach of ASOP No. 27 and the projection resul... outlined above, we are recommending a range for the investment return assumption of the $25^{\text {th }}$ to $75^{\text {th }}$ percentile real returns over the 50 year time span plus the recommended inflation assumption less the recommended expense rate. The following table details the range.

| Item | $\mathbf{2 5}^{\text {th }}$ Percentile | $\mathbf{5 0}^{\text {th }}$ Percentile | $\mathbf{7 5}^{\text {th }}$ Percentile |
| :--- | :--- | :---: | :--- |
| Real Rate of Return* | $3.86 \%$ | $5.29 \%$ | $6.74 \%$ |
| Inflation | $\underline{2.75}$ | $\underline{2.75}$ | $\underline{2.75}$ |
| Net Investment Return | $\mathbf{6 . 6 1 \%}$ | $8.04 \%$ | $\mathbf{9 . 4 9 \%}$ |

* net of investment expenses.

There is a $50 \%$ chance that the net return will be $8.04 \%$ or more over a 50 -year period. A net return of $7.50 \%$ is at the $40^{\text {th }}$ percentile. Although not in the center of the recommended range, in our opinion a return of $7.50 \%$ is conservative yet reasonable. In addition, the most recent Public Fund Survey indicates that the current median return assumptions for the approximately 126 large public plans in the summary is $7.75 \%$. Further, the recent trend in the return assumption of these large plans is toward lower annual rates of return.

After review of past experience for PSERS and future expectation analysis, we are recommending the real rate of return assumption can be increased from $4.50 \%$ to $4.75 \%$. Combining this with our recommendation to lower the price inflation assumption, we recommend the long-term investment return assumption remain at $7.50 \%$.

| Investment Return Assumption |  |  |
| :--- | :--- | :--- |
|  | Current | Recommended |
| Real Rate of Return* | $4.50 \%$ | $4.75 \%$ |
| Inflation | $\underline{3.00}$ | $\underline{2.75}$ |
| Net Investment Return | $7.50 \%$ | $7.50 \%$ |

*Net of Investment Expenses

## Section IV

## Demographic Assumptions

There are several demographic assumptions used in the actuarial valuations performed for the Georgia Public School Employees' Retirement System. They are:

- Rates of Withdrawal
- Rates of Disability Retirement
- Rates of Service Retirement
- Rate of Mortality

The Actuarial Standards Board has issued Actuarial Standard of Practice (ASOP) No. 35, 'Selection of Demographic and Other Noneconomic Assumptions for Measuring Pension Obligations", which provides guidance to actuaries in selecting demographic assumptions for measuring obligations under defined benefit plans. In our opinion, the demographic assumptions recommended in this report have been developed in accordance with ASOP No. 35.

The purpose of a study of demographic experience is to compare what actually happened to the membership during the study period (July 1, 2009, through June 30, 2014) with what was expected to happen based on the assumptions used in the most recent Actuarial Valuations.

Detailed tabulations by age, service and/or gender are performed over the entire study period. These tabulations look at all active and retired members during the period as well as separately annotating those who experience a demographic event, also referred to as a decrement. In addition the tabulation of all members together with the current assumptions permits the calculation of the number of expected decrements during the study period.

If the actual experience differs significantly from the overall expected results, or if the pattern of actual decrements, or rates of decrement, by age, gender, or service does not follow the expected pattern, new assumptions are recommended. Recommended changes usually do not follow the exact actual experience during the observation period. Judgment is required to extrapolate future experience from past trends and current member behavior.

The remainder of this section presents the results of the demographic study. We have prepared tables that show a comparison of the actual and expected decrements and the overall ratio of actual to expected results (A/E Ratios) under the current assumptions. If a change is being proposed, the revised $\mathrm{A} / \mathrm{E}$ Ratios are shown as well.

## RATES OF WITHDRAWAL

## COMPARISON OF ACTUAL AND EXPECTED WITHDRAWALS FROM ACTIVE SERVICE

| $\begin{aligned} & \text { CENTRAL } \\ & \text { AGE } \\ & \text { OF GROUP } \end{aligned}$ | NUMBER OF WITHIDRAWALS |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | MALE |  |  | FEMALE |  |  |
|  | Actual | Expected | Ratio of Actual to Expected | Actual | Expected | Ratio of Actual to Expected |
|  | Withdrawals with less than 5 years of service |  |  |  |  |  |
| 20 | 154 | 135.7 | 1.135 | 74 | 82.3 | 0.899 |
| 25 | 390 | 419.1 | 0.931 | 420 | 447.1 | 0.939 |
| 30 | 314 | 360.9 | 0.870 | 619 | 721.1 | 0.858 |
| 35 | 347 | 366.3 | 0.947 | 875 | 945.8 | 0.925 |
| 40 | 433 | 424.3 | 1.021 | 1,114 | 1,156.0 | 0.964 |
| 45 | 526 | 557.2 | 0.944 | 1,105 | 1,141.7 | 0.968 |
| 50 | 576 | 613.0 | 0.940 | 990 | 1,020.9 | 0.970 |
| 55 | 519 | 535.5 | 0.969 | 753 | 779.2 | 0.966 |
| 60 | 456 | 486.7 | 0.937 | 498 | 485.9 | 1.025 |
| 63 \& Over | 729 | 626.6 | 1.163 | 672 | 443.4 | 1.516 |
| TOTAL | 4,444 | 4,525.3 | 0.982 | 7,120 | 7,223.4 | 0.986 |
|  | Withdrawals with at least 5 but less than 10 years of service |  |  |  |  |  |
| 25 | 44 | 42.2 | 1.043 | 25 | 28.9 | 0.865 |
| 30 | 77 | 103.9 | 0.741 | 138 | 139.4 | 0.990 |
| 35 | 93 | 98.2 | 0.947 | 317 | 319.3 | 0.993 |
| 40 | 122 | 125.5 | 0.972 | 597 | 617.5 | 0.967 |
| 45 | 178 | 179.4 | 0.992 | 678 | 691.7 | 0.980 |
| 50 | 178 | 225.0 | 0.791 | 621 | 668.9 | 0.928 |
| 55 | 231 | 212.5 | 1.087 | 491 | 488.5 | 1.005 |
| 60 | 244 | 228.9 | 1.066 | 417 | 356.7 | 1.169 |
| 63 \& Over | 759 | 455.0 | 1.668 | 793 | 415.7 | 1.908 |
| TOTAL | 1,926 | 1,670.6 | 1.153 | 4,077 | 3,726.6 | 1.094 |
| Withdrawals with 10 or greater years of service |  |  |  |  |  |  |
| 30 | 13 | 18.0 | 0.722 | 6 | 9.2 | 0.652 |
| 35 | 33 | 34.7 | 0.951 | 73 | 65.5 | 1.115 |
| 40 | 67 | 57.7 | 1.161 | 191 | 206.6 | 0.924 |
| 45 | 108 | 106.4 | 1.015 | 454 | 427.3 | 1.062 |
| 50 | 166 | 167.5 | 0.991 | 555 | 625.7 | 0.887 |
| 55 | 166 | 174.9 | 0.949 | 515 | 597.1 | 0.863 |
| 58 \& Over | 67 | 52.5 | 1.276 | 178 | 193.5 | 0.920 |
| TOTAL | 620 | 611.7 | 1.014 | 1,972 | 2,124.9 | 0.928 |

The following graphs show a comparison of the current expected, actual, and proposed rates withdrawal for actives.







The rates of withdrawal adopted by the Board are used to determine the expected number $u$ separations from active service which will occur as a result of resignation or dismissal. The preceding results indicate that during the study period the number of withdrawals varied from the expected in many age categories. We recommend that the rates of withdrawal be revised at this time to more closely reflect the experience of the System and maintain a degree of conservatism.

## COMPARATIVE RATES OF WITHDRAWAL FROM ACTIVE SERVICE

| AGE | RATES OF WITHIDRAWAL |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Present |  |  | Proposed |  |  |
|  | Years Of Service |  |  | Years Of Service |  |  |
|  | 0-4 | 5-9 | 10 + | 0-4 | 5-9 | 10 + |
|  | Male |  |  |  |  |  |
| 20 | 35.00\% |  |  | 37.00\% |  |  |
| 25 | 30.00\% | 17.00\% |  | 28.00\% | 17.00\% |  |
| 30 | 27.00\% | 16.00\% | 14.00\% | 25.00\% | 15.00\% | 12.00\% |
| 35 | 24.00\% | 14.00\% | 9.00\% | 23.00\% | 13.00\% | 9.00\% |
| 40 | 21.00\% | 12.00\% | 7.00\% | 21.00\% | 12.00\% | 7.50\% |
| 45 | 20.00\% | 11.00\% | 6.50\% | 19.00\% | 11.00\% | 6.50\% |
| 50 | 18.00\% | 11.00\% | 6.50\% | 17.00\% | 9.00\% | 6.50\% |
| 55 | 15.00\% | 9.00\% | 6.00\% | 15.00\% | 9.00\% | 6.00\% |
| 60 | 13.00\% | 9.00\% | 0.00\% | 12.00\% | 7.50\% | 0.00\% |
| 64 | 13.00\% | 9.00\% | 0.00\% | 13.50\% | 11.50\% | 0.00\% |
|  | Female |  |  |  |  |  |
| 20 | 34.00\% |  |  | 32.00\% |  |  |
| 25 | 29.00\% | 19.00\% |  | 28.00\% | 18.00\% |  |
| 30 | 24.00\% | 15.00\% | 11.00\% | 23.00\% | 15.00\% | 10.00\% |
| 35 | 20.00\% | 13.00\% | 10.00\% | 19.00\% | 13.00\% | 10.00\% |
| 40 | 17.00\% | 12.00\% | 8.00\% | 17.00\% | 12.00\% | 8.00\% |
| 45 | 16.00\% | 10.00\% | 7.00\% | 15.50\% | 10.00\% | 7.00\% |
| 50 | 14.00\% | 9.00\% | 6.50\% | 14.00\% | 8.50\% | 6.00\% |
| 55 | 12.00\% | 8.00\% | 6.00\% | 12.00\% | 8.00\% | 5.50\% |
| 60 | 11.00\% | 7.00\% | 0.00\% | 11.00\% | 7.50\% | 0.00\% |
| 64 | 11.00\% | 7.00\% | 0.00\% | 12.00\% | 9.00\% | 0.00\% |

## COMPARISON OF ACTUAL AND EXPECTED WITHDRAWALS BASED ON PROPOSED RATES

| $\begin{gathered} \text { CDNTRAL } \\ \text { AGE } \\ \text { OF GROUP } \end{gathered}$ | NUMBER OF WITHIDRAWALS |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | MALE |  |  | FEMALE |  |  |
|  | Actual | Expected | Ratio of Actual to Expected | Actual | Expected | Ratio of Actual to Expected |
|  | Withdrawals with less than 5 years of service |  |  |  |  |  |
| 20 | 154 | 141.7 | 1.087 | 74 | 77.4 | 0.956 |
| 25 | 390 | 396.8 | 0.983 | 420 | 433.6 | 0.969 |
| 30 | 314 | 339.4 | 0.925 | 619 | 685.3 | 0.903 |
| 35 | 347 | 357.1 | 0.972 | 875 | 892.3 | 0.981 |
| 40 | 433 | 424.3 | 1.021 | 1,114 | 1,130.0 | 0.986 |
| 45 | 526 | 529.3 | 0.994 | 1,105 | 1,119.5 | 0.987 |
| 50 | 576 | 585.2 | 0.984 | 990 | 1,014.0 | 0.976 |
| 55 | 519 | 535.5 | 0.969 | 753 | 772.4 | 0.975 |
| 60 | 456 | 460.8 | 0.990 | 498 | 502.0 | 0.992 |
| 63 \& Over | 729 | 650.7 | 1.120 | 672 | 483.7 | 1.389 |
| TOTAL | 4,444 | 4,420.8 | 1.005 | 7,120 | 7,110.2 | 1.001 |
|  | Withdrawals with at least 5 but less than 10 years of service |  |  |  |  |  |
| 25 | 44 | 42.2 | 1.043 | 25 | 27.4 | 0.912 |
| 30 | 77 | 93.8 | 0.821 | 138 | 139.4 | 0.990 |
| 35 | 93 | 93.1 | 0.999 | 317 | 319.3 | 0.993 |
| 40 | 122 | 125.5 | 0.972 | 597 | 607.5 | 0.983 |
| 45 | 178 | 179.4 | 0.992 | 678 | 684.4 | 0.991 |
| 50 | 178 | 203.4 | 0.875 | 621 | 631.7 | 0.983 |
| 55 | 231 | 207.9 | 1.111 | 491 | 488.3 | 1.006 |
| 60 | 244 | 233.3 | 1.046 | 417 | 391.5 | 1.065 |
| 63 \& Over | 759 | 581.4 | 1.305 | 793 | 534.4 | 1.484 |
| TOTAL | 1,926 | 1,760.0 | 1.094 | 4,077 | 3,823.9 | 1.066 |
| Withdrawals with 10 or greater years of service |  |  |  |  |  |  |
| 30 | 13 | 16.2 | 0.802 | 6 | 8.4 | 0.714 |
| 35 | 33 | 33.7 | 0.979 | 73 | 65.5 | 1.115 |
| 40 | 67 | 60.7 | 1.104 | 191 | 206.6 | 0.924 |
| 45 | 108 | 106.4 | 1.015 | 454 | 427.3 | 1.062 |
| 50 | 166 | 167.5 | 0.991 | 555 | 588.8 | 0.943 |
| 55 | 166 | 174.8 | 0.950 | 515 | 554.5 | 0.929 |
| 58 \& Over | 67 | 52.5 | 1.276 | 178 | 182.8 | 0.974 |
| TOTAL | 620 | 611.8 | 1.013 | 1,972 | 2,033.9 | 0.970 |

## RATES OF DISABILITY RETIREMENT

## COMPARISON OF ACTUAL AND EXPECTED DISABILITY RETIREMENTS

| CENTRAL <br> AGE <br> OF GROUP | NUMBER OF DISABILITY RETIREMIENTS |  |  |
| :---: | :---: | :---: | :---: |
|  | Actual | Expected | Ratio of Actual to Expected |
| 37 \& Under | 0 | 0.4 | 0.000 |
| 40 | 1 | 2.5 | 0.400 |
| 45 | 10 | 10.6 | 0.943 |
| 50 | 27 | 29.1 | 0.928 |
| 55 | 60 | 73.5 | 0.816 |
| 60 | 92 | 100.9 | 0.912 |
| TOTAL | 190 | 217.0 | 0.876 |

The following graph shows a comparison of the current expected, actual, and proposed rates of disability retirement.


During the period under investigation, the actual rates of disability retirement were somewhat less than expected over all age groups. However since this is a conservative result, we recommend no change to the rates of disability retirement at this time and will continue to monitor this assumption to see if future changes are needed.

## RATES OF RETIREMENT

## COMPARISON OF ACTUAL AND EXPECTED RETIREMENTS

| AGE | NUMBER OF SERVICE RETIREMIENTS |  |  |
| :---: | :---: | :---: | :---: |
|  | Actual | Expected | Ratio of Actual to Expected |
| 60 \& Under | 316 | 411.5 | 0.768 |
| 61 | 278 | 399.6 | 0.696 |
| 62 | 561 | 568.5 | 0.987 |
| 63 | 374 | 409.1 | 0.914 |
| 64 | 321 | 373.5 | 0.859 |
| 65 | 497 | 524.2 | 0.948 |
| 66 | 424 | 385.8 | 1.099 |
| 67 | 257 | 316.0 | 0.813 |
| 68 | 241 | 275.5 | 0.875 |
| 69 | 257 | 251.0 | 1.024 |
| 70 | 233 | 214.8 | 1.085 |
| 71 | 190 | 168.3 | 1.129 |
| 72 | 154 | 142.0 | 1.085 |
| 73 | 137 | 128.5 | 1.066 |
| 74 | 112 | 109.3 | 1.025 |
| SUBTOTAL | 4,352 | 4,677.6 | 0.930 |
| 75 \& Over | 479 | 1,628.0 | 0.294 |
| TOTAL | 4,831 | 6,305.6 | 0.766 |

The following graph shows a comparison of the present, actual, and proposed rates of servic retirements.


The analysis of the experience reflects that the current assumed rates of retirement over-anticipate retirements at the younger ages and under anticipate retirements at the older ages. We recommend adjustment to the rates to reflect the experience as well as maintain a reasonable degree of margin.

The following table shows a comparison of the present and proposed rates of service retiremen..

COMPARATIVE RATES OF RETIREMENT

| AGE | RATES OF SERVICEREIIREMIDNT |  |
| :---: | :---: | :---: |
|  | Present | Proposed |
|  |  |  |
| 60 | $15.0 \%$ | $13.0 \%$ |
| 61 | $15.0 \%$ | $13.0 \%$ |
| 62 | $22.0 \%$ | $22.0 \%$ |
| 63 | $18.0 \%$ | $17.5 \%$ |
| 64 | $18.0 \%$ | $17.0 \%$ |
| 65 | $28.0 \%$ | $28.0 \%$ |
| 66 | $25.0 \%$ | $27.0 \%$ |
| 67 | $25.0 \%$ | $23.0 \%$ |
| 68 | $25.0 \%$ | $23.0 \%$ |
| 69 | $25.0 \%$ | $26.0 \%$ |
| 70 | $25.0 \%$ | $27.0 \%$ |
| 71 | $25.0 \%$ | $27.0 \%$ |
| 72 | $25.0 \%$ | $27.0 \%$ |
| 73 | $25.0 \%$ | $27.0 \%$ |
| 74 | $25.0 \%$ | $27.0 \%$ |
| 75 | $100.0 \%$ | $100.0 \%$ |
|  |  |  | BASED ON PROPOSED RATES OF RETIREMENT


| AGE | NUMBER OF SERVICE REIIREMIENTS |  |  |
| :---: | :---: | :---: | :---: |
|  | Actual | Expected | Ratio of Actual to Expected |
| 60 \& Under | 316 | 356.6 | 0.886 |
| 61 | 278 | 346.3 | 0.803 |
| 62 | 561 | 568.5 | 0.987 |
| 63 | 374 | 397.8 | 0.940 |
| 64 | 321 | 352.8 | 0.910 |
| 65 | 497 | 524.2 | 0.948 |
| 66 | 424 | 416.6 | 1.018 |
| 67 | 257 | 290.7 | 0.884 |
| 68 | 241 | 253.5 | 0.951 |
| 69 | 257 | 261.0 | 0.985 |
| 70 | 233 | 231.9 | 1.005 |
| 71 | 190 | 181.7 | 1.046 |
| 72 | 154 | 153.4 | 1.004 |
| 73 | 137 | 138.8 | 0.987 |
| 74 | 112 | 118.0 | 0.949 |
| SUBTOTAL | 4,352 | 4,591.8 | 0.948 |
| 75 \& Over | 479 | 1,628.0 | 0.294 |
| TOTAL | 4,831 | 6,219.8 | 0.777 |

## RATES OF PRE-RETIREMENT MORTALITY

## COMPARISON OF ACTUAL AND EXPECTED CASES OF PRE-RETIREMENT MORTALITY

| $\begin{aligned} & \text { CENTRAL } \\ & \text { AGE } \\ & \text { OF GROUP } \end{aligned}$ | NUMBER OF PRE-RETIREMIENT DEATHS |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Proposed Rates |  |  |  |  |  |
|  | MALES |  |  | FEMALES |  |  |
|  | Actual | Expected | Ratio of Actual to Expected | Actual | Expected | Ratio of Actual to Expected |
| 20 | 0 | 0.2 | 0.000 | 0 | 0.1 | 0.000 |
| 25 | 0 | 0.6 | 0.000 | 0 | 0.4 | 0.000 |
| 30 | 3 | 1.1 | 2.727 | 1 | 1.2 | 0.833 |
| 35 | 1 | 2.2 | 0.455 | 0 | 3.8 | 0.000 |
| 40 | 4 | 4.5 | 0.889 | 6 | 10.4 | 0.577 |
| 45 | 6 | 9.9 | 0.606 | 11 | 22.8 | 0.482 |
| 50 | 16 | 19.8 | 0.808 | 15 | 41.5 | 0.361 |
| 55 | 22 | 37.4 | 0.588 | 29 | 64.1 | 0.452 |
| 58 \& OVER | 92 | 404.3 | 0.228 | 65 | 366.5 | 0.177 |
| TOTAL | 144 | 480.0 | 0.300 | 127 | 510.8 | 0.249 |

During the period under investigation, the actual rates of death in active service were significantly less than expected for both males and females at all ages. We recommend that the rates of mortality in active service for both males and females be changed to the RP-2000 Employee Mortality Table projected to 2025 with projection scale BB. The following graphs show a comparison of the present, actual, and proposed rates of pre-retirement mortality.



| AGE | RATES OF MORTALITY |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | MALE |  | FEMALE |  |
|  | Present | Proposed | Present | Proposed |
| 20 | 0.0357\% | 0.0320\% | 0.0191\% | 0.0177\% |
| 25 | 0.0378\% | 0.0349\% | 0.0207\% | 0.0192\% |
| 30 | 0.0499\% | 0.0412\% | 0.0264\% | 0.0245\% |
| 35 | 0.0841\% | 0.0717\% | 0.0475\% | 0.0441\% |
| 40 | 0.1142\% | 0.1001\% | 0.0706\% | 0.0655\% |
| 45 | 0.1616\% | 0.1399\% | 0.1124\% | 0.1043\% |
| 50 | 0.2449\% | 0.1983\% | 0.1676\% | 0.1555\% |
| 55 | 0.4200\% | 0.2810\% | 0.2717\% | 0.2228\% |
| 60 | 0.7676\% | 0.4092\% | 0.5055\% | 0.3058\% |
| 64 | 1.2737\% | 0.5330\% | 0.8619\% | 0.4015\% |

## COMPARISON OF ACTUAL AND EXPECTED CASES <br> OF PRE-RETIREMENT DEATHS BASED ON PROPOSED RATES OF MORTALITY

| $\begin{gathered} \text { CENTRAL } \\ \text { AGE } \\ \text { OF GROUP } \end{gathered}$ | NUMBER OF PRE-RETIREMENT DEATHS |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Proposed Rates |  |  |  |  |  |
|  | MALES |  |  | FEMALES |  |  |
|  | Actual | Expected | Ratio of Actual to Expected | Actual | Expected | Ratio of Actual to Expected |
| 20 | 0 | 0.1 | 0.000 | 0 | 0.1 | 0.000 |
| 25 | 0 | 0.6 | 0.000 | 0 | 0.3 | 0.000 |
| 30 | 3 | 0.9 | 3.333 | 1 | 1.1 | 0.909 |
| 35 | 1 | 1.9 | 0.526 | 0 | 3.5 | 0.000 |
| 40 | 4 | 3.9 | 1.026 | 6 | 9.7 | 0.619 |
| 45 | 6 | 8.6 | 0.698 | 11 | 21.2 | 0.519 |
| 50 | 16 | 16.2 | 0.988 | 15 | 38.1 | 0.394 |
| 55 | 22 | 25.3 | 0.870 | 29 | 51.8 | 0.560 |
| 58 \& OVER | 92 | 192.0 | 0.479 | 65 | 196.8 | 0.330 |
| TOTAL | 144 | 249.5 | 0.577 | 127 | 322.6 | 0.394 |

## RATES OF POST-RETIREMENT MORTALITY

The current basis for rate of post-retirement mortality for service retirees and beneficiaries is the RP-2000 Combined Mortality Table set forward one year for males. The current basis for rate of post-retirement mortality for disability retirees is the RP-2000 Disabled Mortality Table set back two years for males and set forward one year for females. The following shows a comparison of the actual and expected deaths during the study period.

## COMPARISON OF ACTUAL AND EXPECTED CASES OF POST-RETIREMENT DEATHS

| $\begin{aligned} & \text { CENTRAL } \\ & \text { AGE } \\ & \text { OF GROUP } \end{aligned}$ | NUMBER OF DEATHS AMONG SERVICE REIIIRDMIENTS AND BENDFICIARIES |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | MALE |  |  | FEMALE |  |  |
|  | Actual | Expected | Ratio of Actual to Expected | Actual | Expected | Ratio of Actual to Expected |
| 57 \& Under | 10 | 0.8 | 12.500 | 15 | 1.2 | 12.500 |
| 60 | 10 | 4.0 | 2.500 | 26 | 10.4 | 2.500 |
| 65 | 52 | 37.0 | 1.405 | 102 | 89.7 | 1.137 |
| 70 | 102 | 94.2 | 1.083 | 178 | 198.5 | 0.897 |
| 75 | 181 | 162.6 | 1.113 | 269 | 301.5 | 0.892 |
| 80 | 230 | 234.2 | 0.982 | 398 | 375.7 | 1.059 |
| 85 | 190 | 220.1 | 0.863 | 422 | 397.5 | 1.062 |
| 90 | 152 | 147.2 | 1.033 | 415 | 338.2 | 1.227 |
| 93 \& Over | 54 | 57.3 | 0.942 | 266 | 214.3 | 1.241 |
| TOTAL | 981 | 957.4 | 1.025 | 2,091 | 1,927.0 | 1.085 |


| $\begin{aligned} & \text { CENTRAL } \\ & \text { AGE } \\ & \text { OF GROUP } \end{aligned}$ | NUMBER OF DEATHS AMONG DISABILITY RETIREMIENTS |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | MALE |  |  | FEMALE |  |  |
|  | Actual | Expected | Ratio of Actual to Expected | Actual | Expected | Ratio of Actual to Expected |
| 47 \& Under | 2 | 0.5 | 4.000 | 0 | 0.3 | 0.000 |
| 50 | 1 | 1.8 | 0.556 | 5 | 1.2 | 4.167 |
| 55 | 7 | 6.4 | 1.094 | 6 | 6.1 | 0.984 |
| 60 | 10 | 9.8 | 1.020 | 16 | 17.8 | 0.899 |
| 65 | 14 | 11.2 | 1.250 | 35 | 29.0 | 1.207 |
| 70 | 15 | 11.9 | 1.261 | 33 | 39.6 | 0.833 |
| 75 | 7 | 9.6 | 0.729 | 34 | 34.4 | 0.988 |
| 80 | 10 | 7.1 | 1.408 | 24 | 20.3 | 1.182 |
| 85 | 4 | 4.3 | 0.930 | 11 | 8.7 | 1.264 |
| 90 | 2 | 2.1 | 0.952 | 5 | 5.5 | 0.909 |
| 93 \& Over | 1 | 0.2 | 5.000 | 3 | 1.7 | 1.765 |
| TOTAL | 73 | 64.9 | 1.125 | 172 | 164.6 | 1.045 |

Overall, the number of actual deaths among all retirements and beneficiaries was greater than tl. number of deaths expected during the period under investigation. We recommend the RP-2000 Blue-Collar Mortality Table for service retirements and beneficiaries but in order to provide an additional margin for anticipated mortality improvement, we recommend projecting the table to 2025 with projection scale BB and setting the table forward 3 years for males and 2 years for females. Although an updated mortality table and mortality improvement scale have been published by the Society of Actuaries (SOA), the SOA did not include public sector data in the development of these new tables and relied on private sector data only. The SOA is currently reviewing mortality for the public sector and may issue a new table in time for the next experience study.

For the period after disability retirement, we recommend the RP-2000 Disabled Mortality Table projected to 2025 with scale BB set forward 5 years for both males and females. The following graphs show a comparison of the present, actual, and proposed rates of post-retirement mortality.





The following tables show a comparison of the present and proposed rates of post-retireme... mortality.

COMPARATIVE RATES OF POST-RETIREMENT MORTALITY

| AGE | SERVICERETIREMIENTS AND BENDFCIARIIS |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | MALE |  | fevale |  |
|  | Present | Proposed | Present | Proposed |
| 35 | 0.0841\% | 0.1171\% | 0.0475\% | 0.0597\% |
| 40 | 0.1142\% | 0.1476\% | 0.0706\% | 0.0995\% |
| 45 | 0.1616\% | 0.1974\% | 0.1124\% | 0.1484\% |
| 50 | 0.2449\% | 0.3057\% | 0.1676\% | 0.2084\% |
| 55 | 0.4200\% | 0.5644\% | 0.2717\% | 0.2844\% |
| 60 | 0.7676\% | 0.9575\% | 0.5055\% | 0.5014\% |
| 65 | 1.4409\% | 1.4859\% | 0.9706\% | 0.9774\% |
| 70 | 2.4570\% | 2.4262\% | 1.6742\% | 1.7054\% |
| 75 | 4.2169\% | 3.9830\% | 2.8106\% | 2.7288\% |
| 80 | 7.2041\% | 6.5238\% | 4.5879\% | 4.4542\% |
| 85 | 12.2797\% | 10.9551\% | 7.7446\% | 7.5727\% |
| 90 | 19.9769\% | 18.5991\% | 13.1682\% | 12.7995\% |


| AGE | DISABILITY RETIRDVIDNTS |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | MALE |  | FEMALE |  |
|  | Present | Proposed | Present | Proposed |
| 35 | 2.2571\% | 2.0938\% | 0.7450\% | 0.6911\% |
| 40 | 2.2571\% | 2.0938\% | 0.7450\% | 0.6911\% |
| 45 | 2.2571\% | 2.6878\% | 0.8184\% | 1.0700\% |
| 50 | 2.6404\% | 3.2877\% | 1.2477\% | 1.4595\% |
| 55 | 3.2859\% | 3.5271\% | 1.7598\% | 1.6987\% |
| 60 | 3.9334\% | 3.7102\% | 2.2936\% | 2.0725\% |
| 65 | 4.6584\% | 4.2891\% | 2.9594\% | 2.7830\% |
| 70 | 5.6909\% | 5.6244\% | 4.0140\% | 3.8623\% |
| 75 | 7.3292\% | 7.4957\% | 5.5777\% | 5.3473\% |
| 80 | 9.7640\% | 9.7046\% | 7.7135\% | 7.4098\% |
| 85 | 12.8343\% | 13.9099\% | 10.7099\% | 10.6215\% |
| 90 | 16.2186\% | 23.0128\% | 14.9698\% | 16.7340\% |

## COMPARISON OF ACTUAL AND EXPECTED CASES

OF POST-RETIREMENT DEATHS BASED ON PROPOSED RATES OF MORTALITY

| $\begin{aligned} & \text { CENTRAL } \\ & \text { AGE } \\ & \text { OF GROUP } \end{aligned}$ | NUMBER OF DEATHS AMONG SERVICE RETIREMIDNTS AND BENEFICIARIES |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | MALE |  |  | FEMALE |  |  |
|  | Actual | Expected | Ratio of Actual to Expected | Actual | Expected | Ratio of Actual to Expected |
| 57 \& Under | 10 | 1.1 | 9.091 | 15 | 1.4 | 10.714 |
| 60 | 10 | 4.7 | 2.128 | 26 | 10.5 | 2.476 |
| 65 | 52 | 38.6 | 1.347 | 102 | 89.8 | 1.136 |
| 70 | 102 | 93.0 | 1.097 | 178 | 202.3 | 0.880 |
| 75 | 181 | 153.4 | 1.180 | 269 | 293.7 | 0.916 |
| 80 | 230 | 211.5 | 1.087 | 398 | 365.0 | 1.090 |
| 85 | 190 | 196.1 | 0.969 | 422 | 387.2 | 1.090 |
| 90 | 152 | 136.9 | 1.110 | 415 | 328.2 | 1.264 |
| 93 \& Over | 54 | 58.0 | 0.931 | 266 | 213.0 | 1.249 |
| TOTAL | 981 | 893.3 | 1.098 | 2,091 | 1,891.1 | 1.106 |


| CENTRAL <br> AGE <br> OF GROUP | NUMBER OF DEATHS AMONG DISABILITY RETIREMIENTS |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | MALE |  |  | FEMALE |  |  |
|  | Actual | Expected | Ratio of Actual to Expected | Actual | Expected | Ratio of Actual to Expected |
| 47 \& Under | 2 | 0.6 | 3.333 | 0 | 0.3 | 0.000 |
| 50 | 1 | 2.2 | 0.455 | 5 | 1.4 | 3.571 |
| 55 | 7 | 6.8 | 1.029 | 6 | 5.8 | 1.034 |
| 60 | 10 | 9.2 | 1.087 | 16 | 16.1 | 0.994 |
| 65 | 14 | 10.3 | 1.359 | 35 | 27.3 | 1.282 |
| 70 | 15 | 11.7 | 1.282 | 33 | 38.0 | 0.868 |
| 75 | 7 | 9.8 | 0.714 | 34 | 32.9 | 1.033 |
| 80 | 10 | 7.1 | 1.408 | 24 | 19.5 | 1.231 |
| 85 | 4 | 4.7 | 0.851 | 11 | 8.6 | 1.279 |
| 90 | 2 | 2.9 | 0.690 | 5 | 6.1 | 0.820 |
| 93 \& Over | 1 | 0.3 | 3.333 | 3 | 1.9 | 1.579 |
| TOTAL | 73 | 65.6 | 1.113 | 172 | 157.9 | 1.089 |

## Section V

## Other Assumptions and Methods and Administrative Procedures

ADMINISTRATIVE EXPENSES: Currently, the method used for administrative expenses is to add the budgeted expenses for the fiscal year to the normal cost. We recommend no change to this method

AMORTIZATION METHOD: Currently, the unfunded accrued liability is amortized using a level dollar amortization method. We recommend no change to this amortization method.

ASSETS: Currently, the actuarial value of assets recognizes a portion of the difference between the market value of assets and the expected actuarial value of assets, based on the assumed valuation rate of return. The amount recognized each year is $20 \%$ of the difference between market value and expected actuarial value. We recommend maintaining the current smoothing method.

COST OF LIVING: Currently, we assume cost of living increases of $1.5 \%$ semi-annually. We recommend maintaining this assumption.

OPTION FACTORS: The option factors currently used by the Retirement System are based on the mortality tables and investment rate of return (discount rate) used in the valuation. We recommend that the factors be revised to the mortality table recommended in this experience study.

## ASSUMPTION FOR ACTIVE VESTED MEMBERS TERMINATION BENEFITS:

 Currently, we assume that $25 \%$ of active members who terminate with ten or more years of service before retirement will receive a benefit beginning at age 60 and $75 \%$ will receive a refund of member contributions. We recommend changing this to assume that $50 \%$ will receive a benefit and $50 \%$ will receive a refund of member contributions.VALUATION COST METHOD: Currently, the valuation uses the entry age actuarial cost method. This is the most widely used cost method of large public sector plans and has demonstrated the highest degree of stability as compared to alternative methods. We recommend no change to this assumption.

## APPENDIX A

## Historical June CPI (U) Index

| Year | CPI (U) | Year | CPI (U) |
| :---: | :---: | :---: | :---: |
| 1961 | 29.8 | 1988 | 118.0 |
| 1962 | 30.2 | 1989 | 124.1 |
| 1963 | 30.6 | 1990 | 129.9 |
| 1964 | 31.0 | 1991 | 136.0 |
| 1965 | 31.6 | 1992 | 140.2 |
| 1966 | 32.4 | 1993 | 144.4 |
| 1967 | 33.3 | 1994 | 148.0 |
| 1968 | 34.7 | 1995 | 152.5 |
| 1969 | 36.6 | 1996 | 156.7 |
| 1970 | 38.8 | 1997 | 160.3 |
| 1971 | 40.6 | 1998 | 163.0 |
| 1972 | 41.7 | 1999 | 166.2 |
| 1973 | 44.2 | 2000 | 172.4 |
| 1974 | 49.0 | 2001 | 178.0 |
| 1975 | 53.6 | 2002 | 179.9 |
| 1976 | 56.8 | 2003 | 183.7 |
| 1977 | 60.7 | 2004 | 189.7 |
| 1978 | 65.2 | 2005 | 194.5 |
| 1979 | 72.3 | 2006 | 202.9 |
| 1980 | 82.7 | 2007 | 208.352 |
| 1981 | 90.6 | 2008 | 218.815 |
| 1982 | 97.0 | 2009 | 215.693 |
| 1983 | 99.5 | 2010 | 217.965 |
| 1984 | 103.7 | 2011 | 225.722 |
| 1985 | 107.6 | 2012 | 229.478 |
| 1986 | 109.5 | 2013 | 233.504 |
| 1987 | 113.5 | 2014 | 238.343 |

## APPENDIX B

## Capital Market Assumptions and Asset Allocation

## Real Rates of Return and Standard Deviations by Asset Class

| Asset Class | Expected Real Rate of Return | Standard Deviation |
| :--- | :---: | :---: |
| Fixed Income | $0.0 \%$ | $9.0 \%$ |
| Domestic Stocks - Large Cap | $9.0 \%$ | $21.5 \%$ |
| Domestic Stocks - Mid Cap | $12.0 \%$ | $24.5 \%$ |
| Domestic Stocks - Small Cap | $13.5 \%$ | $34.0 \%$ |
| Int'l Stocks - Developed Mkt | $8.0 \%$ | $19.0 \%$ |
| Int'l Stocks - Emerging Mkt | $12.0 \%$ | $27.0 \%$ |
| Alternatives | $10.5 \%$ | $27.5 \%$ |

## Asset Class Correlation Coefficients

| Asset Class | Fixed <br> Income | Domestic <br> Stocks - <br> Large <br> Cap | Domestic <br> Stocks - <br> Mid <br> Cap | Domestic <br> Stocks - <br> Small <br> Cap | Int'l <br> Stocks - <br> Developed <br> Mkt | Int'l <br> Stocks - <br> Emerging <br> Mkt | Alts |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Fixed Income | 1.00 |  |  |  |  |  |  |
| Domestic Stocks - Large Cap | 0.18 | 1.00 |  |  |  |  |  |
| Domestic Stocks - Mid Cap | 0.18 | 0.94 | 1.00 |  |  |  |  |
| Domestic Stocks - Small Cap | 0.14 | 0.83 | 0.90 | 1.00 |  |  |  |
| Int'l Stocks - Developed Mkt | 0.15 | 0.63 | 0.65 | 0.51 | 1.00 |  |  |
| Int'l Stocks - Emerging Mkt | 0.08 | 0.67 | 0.70 | 0.65 | 0.69 | 1.00 |  |
| Alternatives | 0.32 | 0.75 | 0.80 | 0.83 | 0.65 | 0.63 | 1.00 |

## Asset Allocation Targets

| Asset Class | Asset Allocation |
| :--- | :---: |
| Fixed Income | $30.0 \%$ |
| US Large Stocks | $39.7 \%$ |
| US Mid Stocks | $3.7 \%$ |
| US Small Stocks | $1.6 \%$ |
| Int'l Developed Mkt Stocks | $18.9 \%$ |
| Int'l Emerging Mkt Stocks | $6.1 \%$ |

## APPENDIX C

TABLE 1
RATES OF SEPARATION FROM ACTIVE SERVICE - MALES

| AGE | Rates of Withdrawal |  |  | Death | Disability | Retirement |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Service |  |  |  |  |  |
|  | 0-4 | 5-9 | 10+ |  |  |  |
| 19 | 0.37000 |  |  | 0.000307 |  |  |
| 20 | 0.37000 |  |  | 0.000320 |  |  |
| 21 | 0.36000 |  |  | 0.000331 |  |  |
| 22 | 0.34000 |  |  | 0.000340 |  |  |
| 23 | 0.29000 | 0.17000 |  | 0.000346 |  |  |
| 24 | 0.29000 | 0.17000 |  | 0.000349 |  |  |
| 25 | 0.28000 | 0.17000 |  | 0.000349 |  |  |
| 26 | 0.28000 | 0.17000 |  | 0.000351 |  |  |
| 27 | 0.28000 | 0.17000 |  | 0.000354 |  |  |
| 28 | 0.27000 | 0.16000 | 0.13500 | 0.000365 |  |  |
| 29 | 0.26000 | 0.15000 | 0.13000 | 0.000382 |  |  |
| 30 | 0.25000 | 0.15000 | 0.12000 | 0.000412 |  |  |
| 31 | 0.24000 | 0.14000 | 0.12000 | 0.000463 | 0.000005 |  |
| 32 | 0.24000 | 0.14000 | 0.12000 | 0.000521 | 0.000005 |  |
| 33 | 0.24000 | 0.14000 | 0.11000 | 0.000585 | 0.000010 |  |
| 34 | 0.24000 | 0.13000 | 0.10000 | 0.000651 | 0.000010 |  |
| 35 | 0.23000 | 0.13000 | 0.09000 | 0.000717 | 0.000025 |  |
| 36 | 0.23000 | 0.13000 | 0.09000 | 0.000780 | 0.000035 |  |
| 37 | 0.22000 | 0.12000 | 0.08000 | 0.000839 | 0.000050 |  |
| 38 | 0.22000 | 0.12000 | 0.08000 | 0.000894 | 0.000080 |  |
| 39 | 0.22000 | 0.12000 | 0.08000 | 0.000947 | 0.000095 |  |
| 40 | 0.21000 | 0.12000 | 0.07500 | 0.001001 | 0.000110 |  |
| 41 | 0.21000 | 0.12000 | 0.07500 | 0.001059 | 0.000160 |  |
| 42 | 0.20000 | 0.12000 | 0.07000 | 0.001127 | 0.000215 |  |
| 43 | 0.19000 | 0.11000 | 0.07000 | 0.001205 | 0.000270 |  |
| 44 | 0.19000 | 0.11000 | 0.06500 | 0.001296 | 0.000320 |  |
| 45 | 0.19000 | 0.11000 | 0.06500 | 0.001399 | 0.000370 |  |
| 46 | 0.19000 | 0.11000 | 0.06500 | 0.001499 | 0.000465 |  |
| 47 | 0.19000 | 0.11000 | 0.06500 | 0.001609 | 0.000565 |  |
| 48 | 0.19000 | 0.11000 | 0.06500 | 0.001725 | 0.000665 |  |
| 49 | 0.18000 | 0.10000 | 0.06500 | 0.001851 | 0.000765 |  |
| 50 | 0.17000 | 0.09000 | 0.06500 | 0.001983 | 0.000865 |  |
| 51 | 0.16000 | 0.09000 | 0.06500 | 0.002122 | 0.001015 |  |
| 52 | 0.16000 | 0.09000 | 0.06500 | 0.002271 | 0.001165 |  |
| 53 | 0.16000 | 0.09000 | 0.06500 | 0.002431 | 0.001750 |  |
| 54 | 0.16000 | 0.09000 | 0.06000 | 0.002609 | 0.002000 |  |
| 55 | 0.15000 | 0.09000 | 0.06000 | 0.002810 | 0.002250 |  |
| 56 | 0.15000 | 0.09000 | 0.05500 | 0.003067 | 0.002500 |  |
| 57 | 0.13000 | 0.09000 | 0.05000 | 0.003282 | 0.003000 |  |
| 58 | 0.12000 | 0.09000 | 0.04500 | 0.003526 | 0.003250 |  |
| 59 | 0.12000 | 0.08500 | 0.04500 | 0.003797 | 0.003500 |  |
| 60 | 0.12000 | 0.07500 |  | 0.004092 | 0.003500 | 0.13000 |
| 61 | 0.12000 | 0.09000 |  | 0.004403 | 0.003500 | 0.13000 |
| 62 | 0.13500 | 0.11500 |  | 0.004721 | 0.003500 | 0.22000 |
| 63 | 0.13500 | 0.11500 |  | 0.005034 | 0.003500 | 0.17500 |
| 64 | 0.13500 | 0.11500 |  | 0.005330 | 0.003500 | 0.17000 |
| 65 | 0.13500 | 0.11500 |  | 0.005600 |  | 0.28000 |
| 66 | 0.13500 | 0.11500 |  | 0.005839 |  | 0.27000 |
| 67 | 0.13500 | 0.11500 |  | 0.006044 |  | 0.23000 |
| 68 | 0.13500 | 0.11500 |  | 0.006215 |  | 0.23000 |
| 69 | 0.13500 | 0.11500 |  | 0.006518 |  | 0.26000 |
| 70 | 0.13500 | 0.11500 |  | 0.006800 |  | 0.27000 |
| 71 | 0.13500 | 0.11500 |  | 0.016839 |  | 0.27000 |
| 72 | 0.13500 | 0.11500 |  | 0.018697 |  | 0.27000 |
| 73 | 0.13500 | 0.11500 |  | 0.020825 |  | 0.27000 |
| 74 | 0.13500 | 0.11500 |  | 0.023233 |  | 0.27000 |
| 75 | 0.00000 | 0.00000 |  | 0.025929 |  | 1.00000 |

TABLE 2
RATES OF SEPARATION FROM ACTIVE SERVICE - FEMALES

| AGE | Rates of Withdrawal |  |  | Death | Disability | Retirement |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Service |  |  |  |  |  |
|  | 0-4 | 5-9 | 10+ |  |  |  |
| 19 | 0.32000 |  |  | 0.000176 |  |  |
| 20 | 0.32000 |  |  | 0.000177 |  |  |
| 21 | 0.32000 |  |  | 0.000178 |  |  |
| 22 | 0.32000 |  |  | 0.000180 |  |  |
| 23 | 0.32000 | 0.18000 |  | 0.000183 |  |  |
| 24 | 0.30000 | 0.18000 |  | 0.000186 |  |  |
| 25 | 0.28000 | 0.18000 |  | 0.000192 |  |  |
| 26 | 0.28000 | 0.18000 |  | 0.000199 |  |  |
| 27 | 0.26000 | 0.18000 |  | 0.000207 |  |  |
| 28 | 0.25000 | 0.15000 | 0.10000 | 0.000218 |  |  |
| 29 | 0.23000 | 0.15000 | 0.10000 | 0.000230 |  |  |
| 30 | 0.23000 | 0.15000 | 0.10000 | 0.000245 |  |  |
| 31 | 0.22000 | 0.15000 | 0.10000 | 0.000285 | 0.000005 |  |
| 32 | 0.21000 | 0.15000 | 0.10000 | 0.000325 | 0.000005 |  |
| 33 | 0.20000 | 0.14000 | 0.10000 | 0.000365 | 0.000010 |  |
| 34 | 0.19000 | 0.13000 | 0.10000 | 0.000404 | 0.000010 |  |
| 35 | 0.19000 | 0.13000 | 0.10000 | 0.000441 | 0.000025 |  |
| 36 | 0.19000 | 0.13000 | 0.10000 | 0.000477 | 0.000035 |  |
| 37 | 0.18000 | 0.12500 | 0.10000 | 0.000514 | 0.000050 |  |
| 38 | 0.18000 | 0.12000 | 0.09000 | 0.000555 | 0.000080 |  |
| 39 | 0.18000 | 0.12000 | 0.09000 | 0.000601 | 0.000095 |  |
| 40 | 0.17000 | 0.12000 | 0.08000 | 0.000655 | 0.000110 |  |
| 41 | 0.16000 | 0.12000 | 0.08000 | 0.000718 | 0.000160 |  |
| 42 | 0.16000 | 0.11000 | 0.08000 | 0.000790 | 0.000215 |  |
| 43 | 0.16000 | 0.11000 | 0.08000 | 0.000869 | 0.000270 |  |
| 44 | 0.16000 | 0.10500 | 0.07000 | 0.000955 | 0.000320 |  |
| 45 | 0.15500 | 0.10000 | 0.07000 | 0.001043 | 0.000370 |  |
| 46 | 0.15000 | 0.10000 | 0.07000 | 0.001135 | 0.000465 |  |
| 47 | 0.15000 | 0.09000 | 0.07000 | 0.001230 | 0.000565 |  |
| 48 | 0.15000 | 0.09000 | 0.06500 | 0.001330 | 0.000665 |  |
| 49 | 0.14000 | 0.08500 | 0.06000 | 0.001438 | 0.000765 |  |
| 50 | 0.14000 | 0.08500 | 0.06000 | 0.001555 | 0.000865 |  |
| 51 | 0.14000 | 0.08500 | 0.06000 | 0.001683 | 0.001015 |  |
| 52 | 0.13500 | 0.08000 | 0.06000 | 0.001825 | 0.001165 |  |
| 53 | 0.13500 | 0.08000 | 0.05500 | 0.001981 | 0.001750 |  |
| 54 | 0.13000 | 0.08000 | 0.05500 | 0.002100 | 0.002000 |  |
| 55 | 0.12000 | 0.08000 | 0.05500 | 0.002228 | 0.002250 |  |
| 56 | 0.12000 | 0.07500 | 0.05000 | 0.002371 | 0.002500 |  |
| 57 | 0.11000 | 0.07500 | 0.04500 | 0.002525 | 0.003000 |  |
| 58 | 0.11000 | 0.07500 | 0.04500 | 0.002692 | 0.003250 |  |
| 59 | 0.11000 | 0.07500 | 0.04000 | 0.002871 | 0.003500 |  |
| 60 | 0.11000 | 0.07500 |  | 0.003058 | 0.003500 | 0.13000 |
| 61 | 0.12000 | 0.07500 |  | 0.003250 | 0.003500 | 0.13000 |
| 62 | 0.12000 | 0.08500 |  | 0.003443 | 0.003500 | 0.22000 |
| 63 | 0.12000 | 0.09000 |  | 0.003726 | 0.003500 | 0.17500 |
| 64 | 0.12000 | 0.09000 |  | 0.004015 | 0.003500 | 0.17000 |
| 65 | 0.12000 | 0.09000 |  | 0.004304 |  | 0.28000 |
| 66 | 0.12000 | 0.09000 |  | 0.004590 |  | 0.27000 |
| 67 | 0.12000 | 0.09000 |  | 0.004868 |  | 0.23000 |
| 68 | 0.12000 | 0.09000 |  | 0.005136 |  | 0.23000 |
| 69 | 0.12000 | 0.09000 |  | 0.005390 |  | 0.26000 |
| 70 | 0.12000 | 0.09000 |  | 0.005630 |  | 0.27000 |
| 71 | 0.12000 | 0.09000 |  | 0.013739 |  | 0.27000 |
| 72 | 0.12000 | 0.09000 |  | 0.015281 |  | 0.27000 |
| 73 | 0.12000 | 0.09000 |  | 0.016986 |  | 0.27000 |
| 74 | 0.12000 | 0.09000 |  | 0.018826 |  | 0.27000 |
| 75 | 0.00000 | 0.00000 |  | 0.020784 |  | 1.00000 |

TABLE 3
RATES OF MORTALITY FOR MEMBERS RETIRED ON ACCOUNT OF SERVICE AND BENEFICIARIES OF DECEASED MEMBERS

| AGE | MALES | FEMALES | AGE | MALES | FEMALES |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 19 | 0.000340 | 0.000178 | 71 | 0.026765 | 0.018905 |
| 20 | 0.000346 | 0.000180 | 72 | 0.029559 | 0.020840 |
| 21 | 0.000349 | 0.000183 | 73 | 0.032686 | 0.022841 |
| 22 | 0.000349 | 0.000186 | 74 | 0.036100 | 0.024982 |
| 23 | 0.000351 | 0.000192 | 75 | 0.039830 | 0.027288 |
| 24 | 0.000354 | 0.000199 | 76 | 0.043908 | 0.029886 |
| 25 | 0.000365 | 0.000207 | 77 | 0.048349 | 0.032811 |
| 26 | 0.000382 | 0.000218 | 78 | 0.053569 | 0.036200 |
| 27 | 0.000673 | 0.000230 | 79 | 0.059187 | 0.040104 |
| 28 | 0.000742 | 0.000272 | 80 | 0.065238 | 0.044542 |
| 29 | 0.000812 | 0.000304 | 81 | 0.071733 | 0.049549 |
| 30 | 0.000880 | 0.000340 | 82 | 0.078867 | 0.055210 |
| 31 | 0.000945 | 0.000383 | 83 | 0.086598 | 0.061450 |
| 32 | 0.001008 | 0.000429 | 84 | 0.097448 | 0.068280 |
| 33 | 0.001067 | 0.000481 | 85 | 0.109551 | 0.075727 |
| 34 | 0.001119 | 0.000537 | 86 | 0.122941 | 0.083791 |
| 35 | 0.001171 | 0.000597 | 87 | 0.137847 | 0.092252 |
| 36 | 0.001220 | 0.000663 | 88 | 0.152743 | 0.103665 |
| 37 | 0.001272 | 0.000736 | 89 | 0.168812 | 0.115625 |
| 38 | 0.001330 | 0.000814 | 90 | 0.185991 | 0.127995 |
| 39 | 0.001399 | 0.000901 | 91 | 0.204007 | 0.140681 |
| 40 | 0.001476 | 0.000995 | 92 | 0.223224 | 0.153204 |
| 41 | 0.001564 | 0.001091 | 93 | 0.250467 | 0.165667 |
| 42 | 0.001663 | 0.001189 | 94 | 0.271263 | 0.181190 |
| 43 | 0.001757 | 0.001287 | 95 | 0.285234 | 0.194718 |
| 44 | 0.001861 | 0.001384 | 96 | 0.306313 | 0.202595 |
| 45 | 0.001974 | 0.001484 | 97 | 0.319624 | 0.214644 |
| 46 | 0.002100 | 0.001588 | 98 | 0.341120 | 0.220284 |
| 47 | 0.002237 | 0.001699 | 99 | 0.353540 | 0.232882 |
| 48 | 0.002545 | 0.001821 | 100 | 0.373578 | 0.242074 |
| 49 | 0.002778 | 0.001946 | 101 | 0.382320 | 0.259472 |
| 50 | 0.003057 | 0.002084 | 102 | 0.397886 | 0.272162 |
| 51 | 0.003379 | 0.002234 | 103 | 0.400000 | 0.293116 |
| 52 | 0.003892 | 0.002342 | 104 | 0.400000 | 0.307811 |
| 53 | 0.004608 | 0.002466 | 105 | 0.400000 | 0.322725 |
| 54 | 0.005092 | 0.002632 | 106 | 0.400000 | 0.337441 |
| 55 | 0.005644 | 0.002844 | 107 | 0.400000 | 0.351544 |
| 56 | 0.006244 | 0.003107 | 108 | 0.400000 | 0.364617 |
| 57 | 0.006938 | 0.003437 | 109 | 0.400000 | 0.376246 |
| 58 | 0.007713 | 0.003849 | 110 | 0.400000 | 0.386015 |
| 59 | 0.008594 | 0.004394 | 111 | 0.400000 | 0.393507 |
| 60 | 0.009575 | 0.005014 | 112 | 0.400000 | 0.398308 |
| 61 | 0.010474 | 0.005900 | 113 | 0.400000 | 0.400000 |
| 62 | 0.011491 | 0.006755 | 114 | 0.400000 | 0.400000 |
| 63 | 0.012656 | 0.007689 | 115 | 0.400000 | 0.400000 |
| 64 | 0.013737 | 0.008754 | 116 | 0.400000 | 0.400000 |
| 65 | 0.014859 | 0.009774 | 117 | 1.000000 | 0.400000 |
| 66 | 0.016410 | 0.010882 | 118 | 1.000000 | 1.000000 |
| 67 | 0.018338 | 0.012118 | 119 | 1.000000 | 1.000000 |
| 68 | 0.020106 | 0.013779 | 120 | 1.000000 | 1.000000 |
| 69 | 0.022062 | 0.015332 |  |  |  |
| 70 | 0.024262 | 0.017054 |  |  |  |

TABLE 4
RATES OF MORTALITY FOR MEMBERS RETIRED ON ACCOUNT OF DISABILITY

| AGE | MALES | FEMALES | AGE | MALES | FEMALES |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 19 | 0.020938 | 0.006911 | 71 | 0.059591 | 0.041246 |
| 20 | 0.020938 | 0.006911 | 72 | 0.063153 | 0.044032 |
| 21 | 0.020938 | 0.006911 | 73 | 0.066917 | 0.046990 |
| 22 | 0.020938 | 0.006911 | 74 | 0.070859 | 0.050131 |
| 23 | 0.020938 | 0.006911 | 75 | 0.074957 | 0.053473 |
| 24 | 0.020938 | 0.006911 | 76 | 0.079187 | 0.057039 |
| 25 | 0.020938 | 0.006911 | 77 | 0.083527 | 0.060857 |
| 26 | 0.020938 | 0.006911 | 78 | 0.087959 | 0.064954 |
| 27 | 0.020938 | 0.006911 | 79 | 0.092468 | 0.069358 |
| 28 | 0.020938 | 0.006911 | 80 | 0.097046 | 0.074098 |
| 29 | 0.020938 | 0.006911 | 81 | 0.101687 | 0.079197 |
| 30 | 0.020938 | 0.006911 | 82 | 0.109122 | 0.084679 |
| 31 | 0.020938 | 0.006911 | 83 | 0.116934 | 0.090559 |
| 32 | 0.020938 | 0.006911 | 84 | 0.125144 | 0.096851 |
| 33 | 0.020938 | 0.006911 | 85 | 0.139099 | 0.106215 |
| 34 | 0.020938 | 0.006911 | 86 | 0.155385 | 0.116438 |
| 35 | 0.020938 | 0.006911 | 87 | 0.172787 | 0.127572 |
| 36 | 0.020938 | 0.006911 | 88 | 0.191152 | 0.139427 |
| 37 | 0.020938 | 0.006911 | 89 | 0.210317 | 0.153358 |
| 38 | 0.020938 | 0.006911 | 90 | 0.230128 | 0.167340 |
| 39 | 0.020938 | 0.006911 | 91 | 0.250467 | 0.181190 |
| 40 | 0.020938 | 0.006911 | 92 | 0.271263 | 0.194718 |
| 41 | 0.022121 | 0.007592 | 93 | 0.285234 | 0.202595 |
| 42 | 0.023306 | 0.008311 | 94 | 0.306313 | 0.214644 |
| 43 | 0.024493 | 0.009068 | 95 | 0.319624 | 0.220284 |
| 44 | 0.025684 | 0.009865 | 96 | 0.341120 | 0.232882 |
| 45 | 0.026878 | 0.010700 | 97 | 0.353540 | 0.242074 |
| 46 | 0.028078 | 0.011574 | 98 | 0.373578 | 0.259472 |
| 47 | 0.029279 | 0.012482 | 99 | 0.382320 | 0.272162 |
| 48 | 0.030481 | 0.013418 | 100 | 0.397886 | 0.293116 |
| 49 | 0.031681 | 0.014019 | 101 | 0.400000 | 0.307811 |
| 50 | 0.032877 | 0.014595 | 102 | 0.400000 | 0.322725 |
| 51 | 0.034074 | 0.015140 | 103 | 0.400000 | 0.337441 |
| 52 | 0.034400 | 0.015650 | 104 | 0.400000 | 0.351544 |
| 53 | 0.034701 | 0.016124 | 105 | 0.400000 | 0.364617 |
| 54 | 0.034987 | 0.016567 | 106 | 0.400000 | 0.376246 |
| 55 | 0.035271 | 0.016987 | 107 | 0.400000 | 0.386015 |
| 56 | 0.035565 | 0.017395 | 108 | 0.400000 | 0.393507 |
| 57 | 0.035881 | 0.017807 | 109 | 0.400000 | 0.398308 |
| 58 | 0.036234 | 0.018704 | 110 | 0.400000 | 0.400000 |
| 59 | 0.036637 | 0.019670 | 111 | 0.400000 | 0.400000 |
| 60 | 0.037102 | 0.020725 | 112 | 0.400000 | 0.400000 |
| 61 | 0.037645 | 0.021884 | 113 | 0.400000 | 0.400000 |
| 62 | 0.038275 | 0.023164 | 114 | 0.400000 | 0.400000 |
| 63 | 0.039002 | 0.024576 | 115 | 1.000000 | 1.000000 |
| 64 | 0.040855 | 0.026129 | 116 | 1.000000 | 1.000000 |
| 65 | 0.042891 | 0.027830 | 117 | 1.000000 | 1.000000 |
| 66 | 0.045123 | 0.029683 | 118 | 1.000000 | 1.000000 |
| 67 | 0.047566 | 0.031687 | 119 | 1.000000 | 1.000000 |
| 68 | 0.050230 | 0.033845 | 120 | 1.000000 | 1.000000 |
| 69 | 0.053122 | 0.036157 |  |  |  |
| 70 | 0.056244 | 0.038623 |  |  |  |


[^0]:    *Net of Investment Expenses

